

# Microturbulence within the front of a quasi-perpendicular supercritical shock

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B. Lembège<sup>(1)</sup> and Muschietti L.<sup>(1, 2)</sup>

(1): LATMOS, UVSQ, Guyancourt, France;

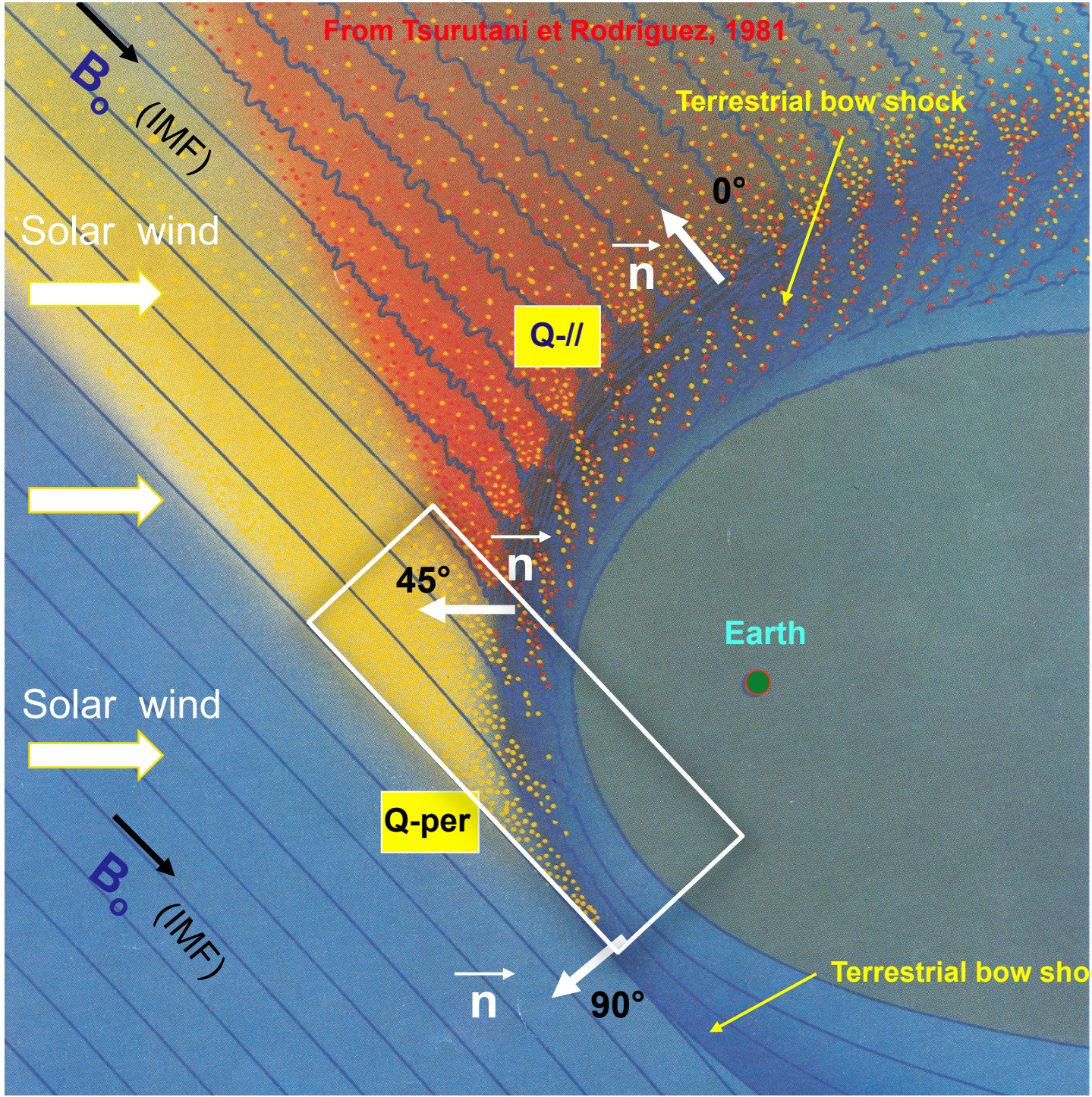
(2): SSL, UC Berkeley, USA

## Motivations:

- \* To focuss on wave activity within a shock front, in particular
  - > in foot region
  - > within  $\Omega_{ce}$  range
- \* What main source mechanisms ?
- \* To analyze in details their linear and nonlinear features ?
- \* Impact of microturbulence on preheating in the foot ?



From Tsurutani et Rodriguez, 1981



$$\theta_{Bv} = (\vec{n}, \vec{B}_o)$$

- $\vec{n}$  = shock front normal
- $\vec{B}_o$  = interplanetary magnetic field (IMF)

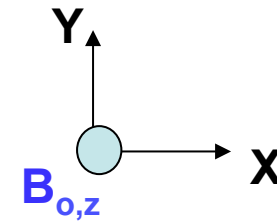
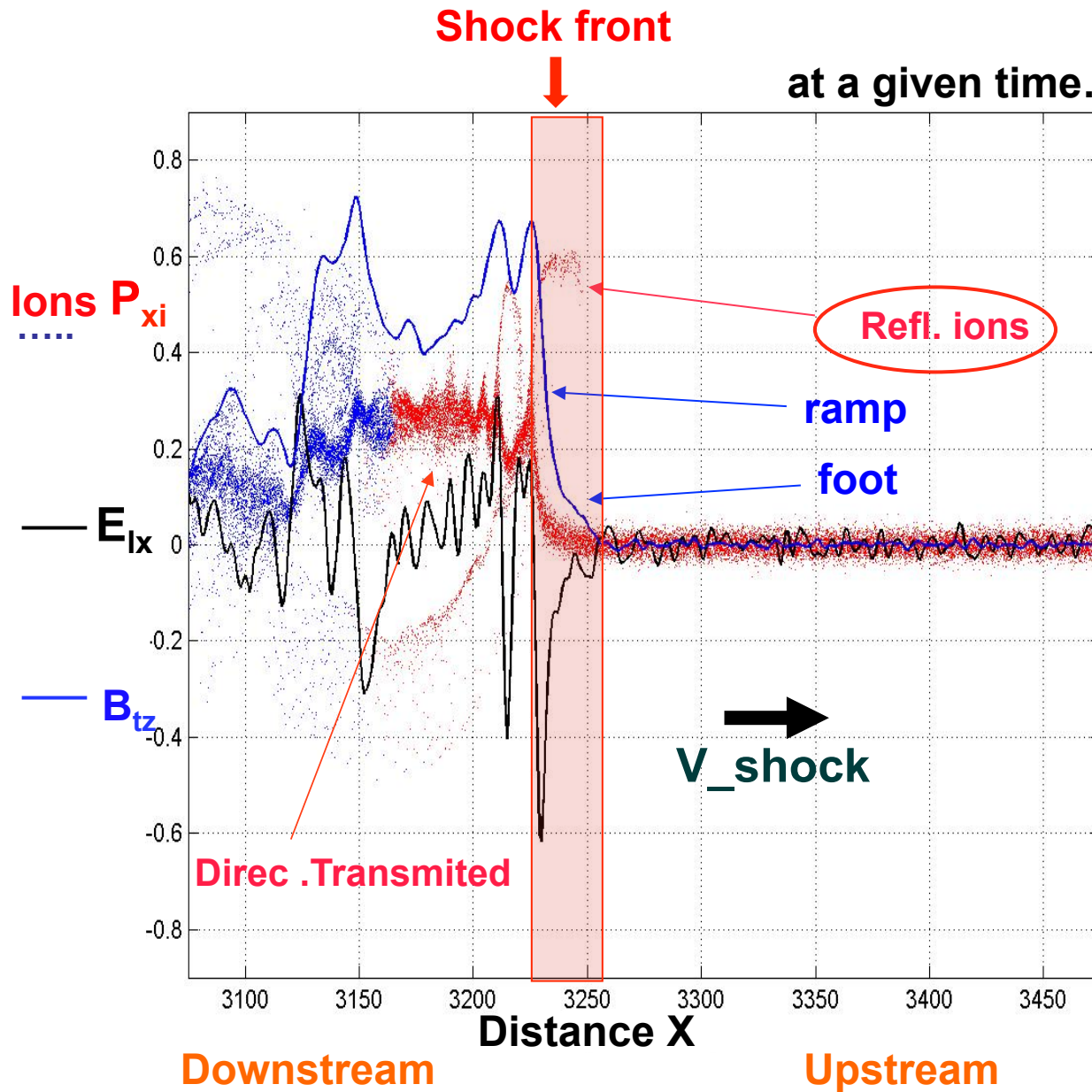


1D PIC simulation of shock:  $90^\circ$ ,  $Ma= 4.3$  ,  $\beta_i= 0.022$

Supercritical shock

at a given time.....

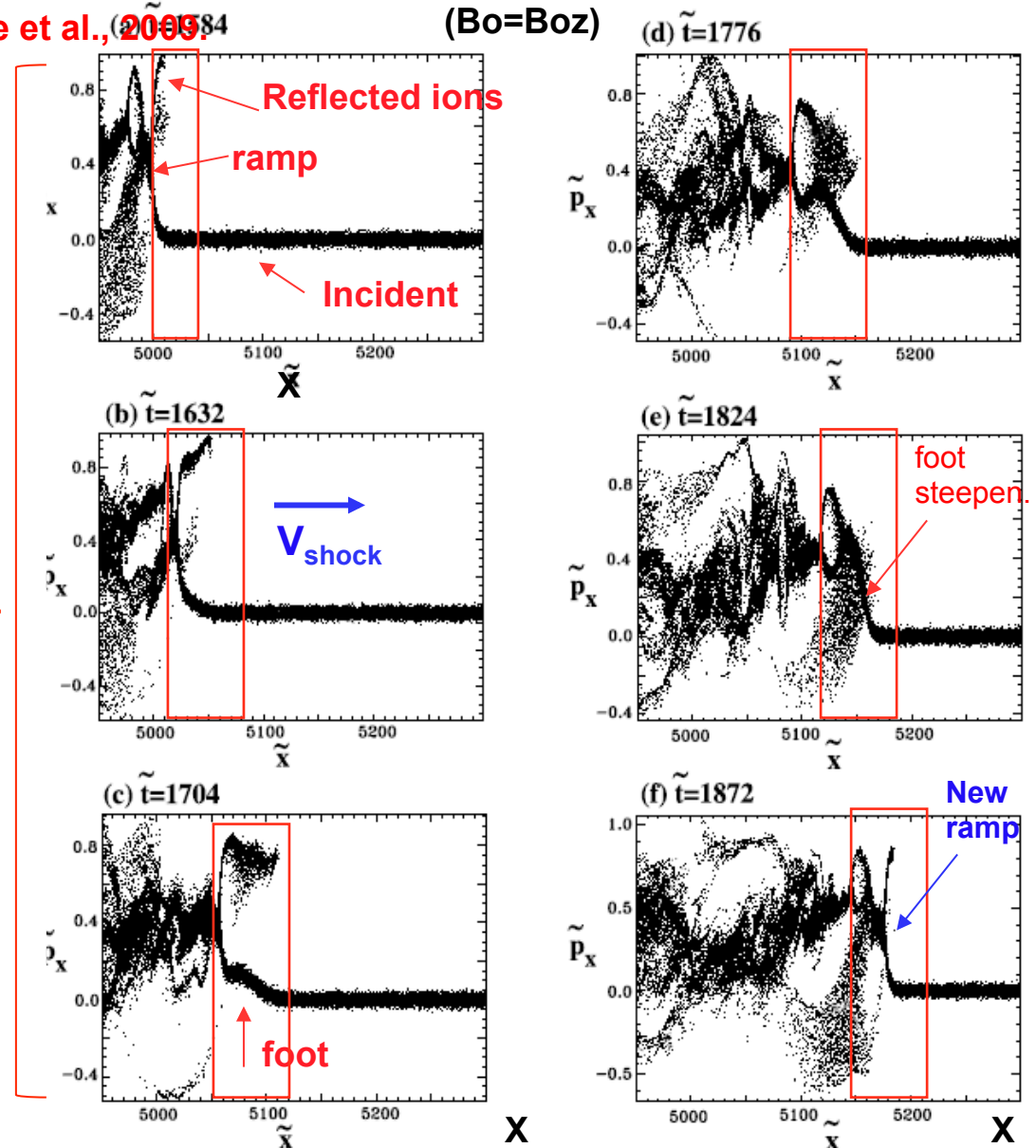
E x B effect



# The shock front self-reformation: an example of front nonstationarity

**PIC simul.:** Biskamp et Welter, 1972; Lembege et Dawson, 1987; Lembege et Savoini, 1992; Schmitz et al., 2002; Lee et Chapman, 2005

**Hybrid simul.:** Hellinger et al. 2002, Lembege et al., 2009



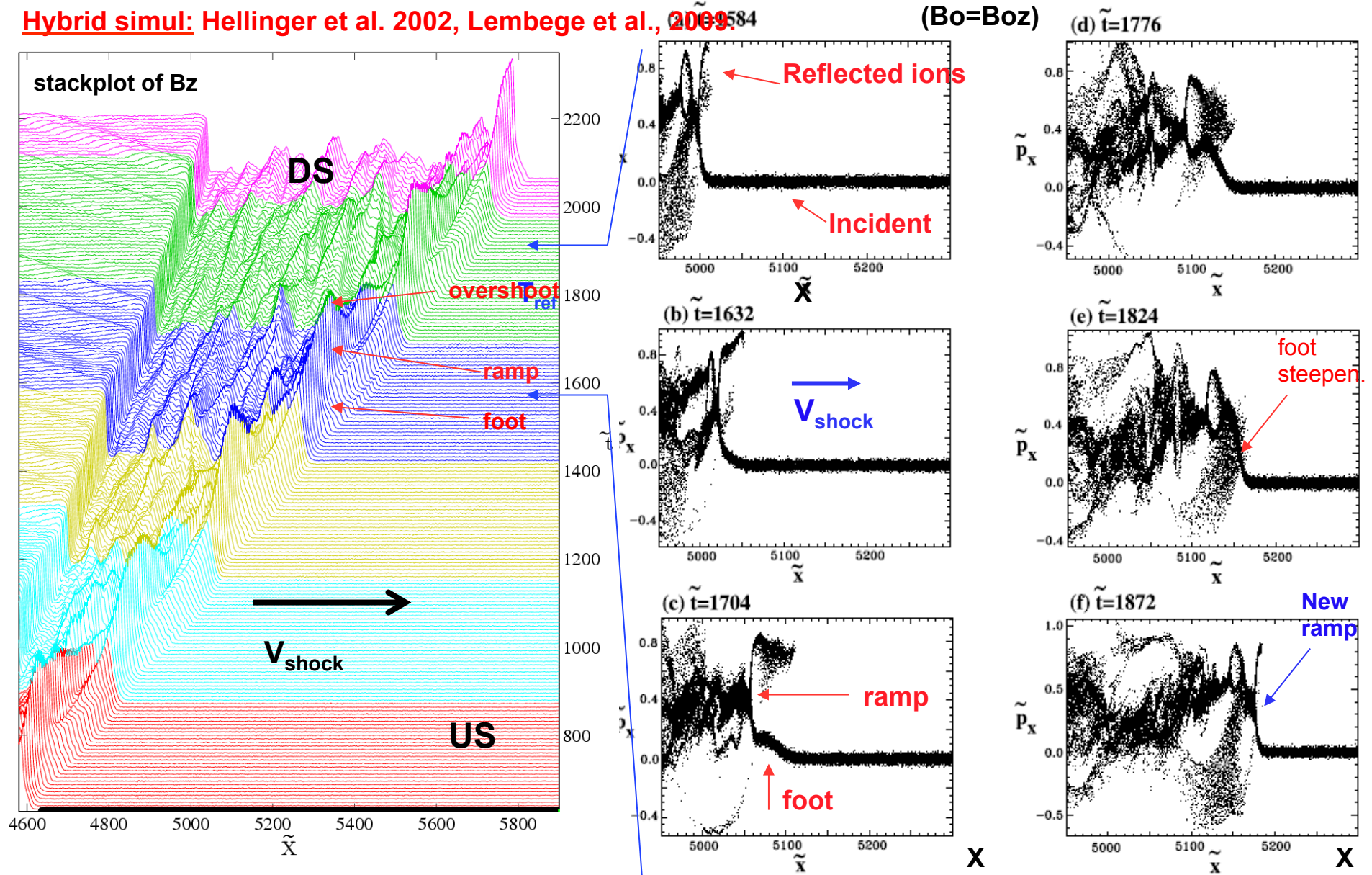
« Self-reformation »  
of the shock front



# The shock front self-reformation: an example of front nonstationarity

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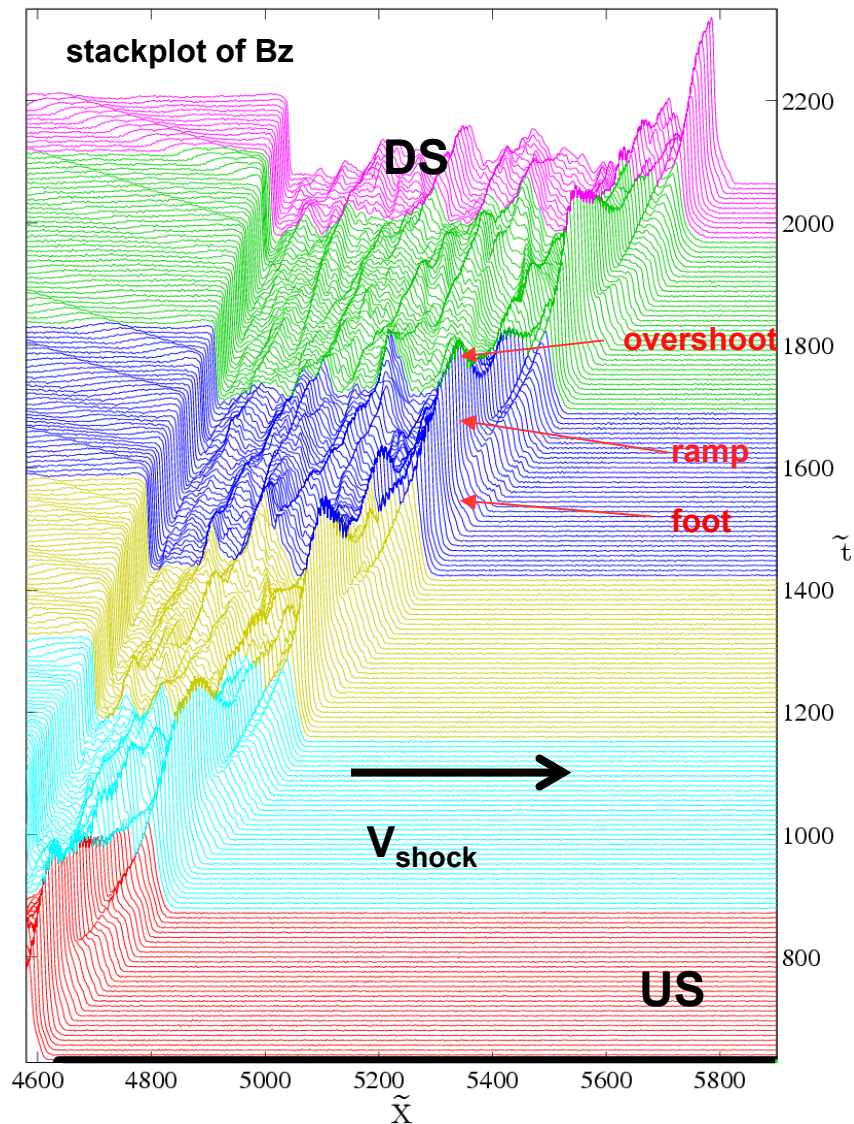
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# The shock front self-reformation: an example of front nonstationarity

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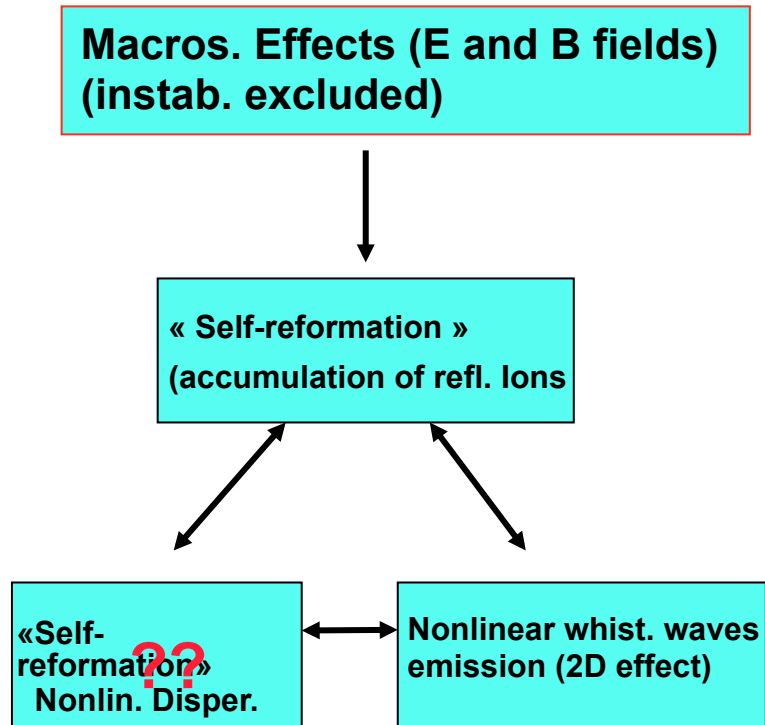


i) This self-reformation process persists  
\* in 1D/ 2D/ 3D  
\* with hybrid / PIC simul.

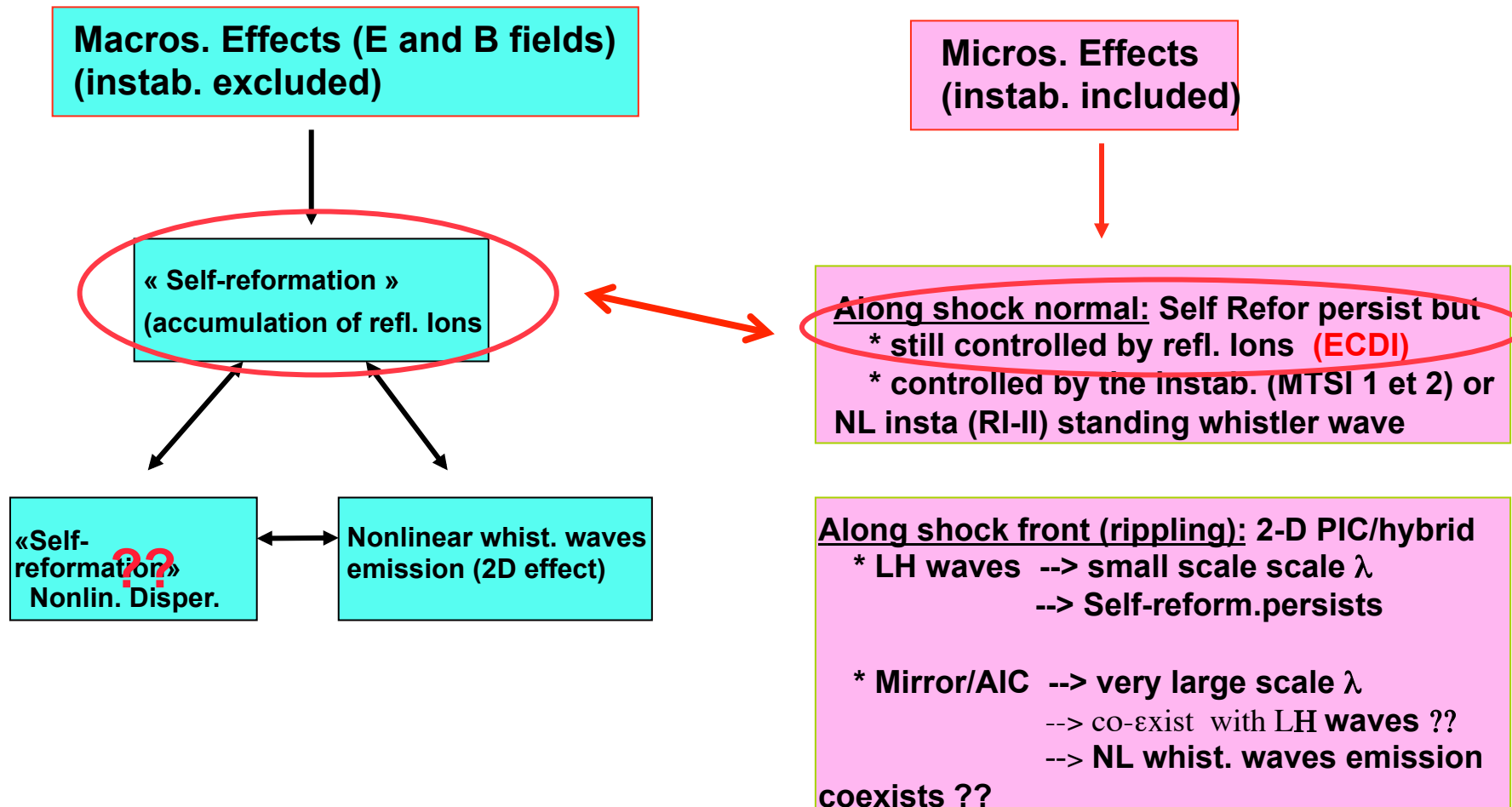
ii) Self reform time period:  $0.3 \tau_{\text{ci,us}}$   
→ 2-3 cycles within one  $\tau_{\text{ci,us}}$



## Sources of nonstationarity (Q-perp Shock)



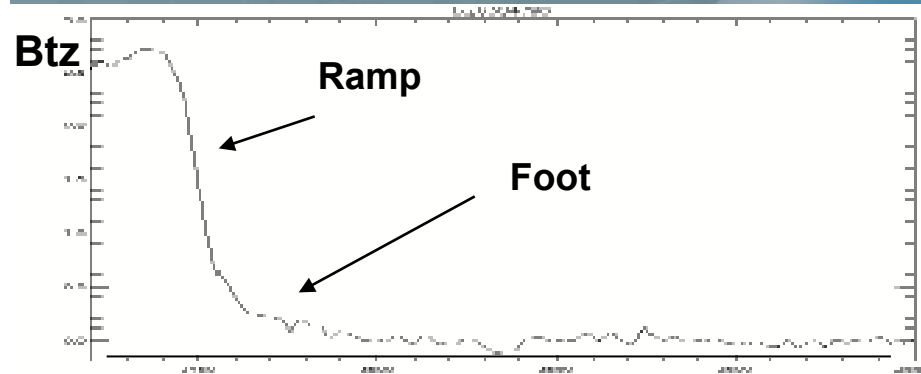
## Sources of nonstationarity (Q-perp Shock)



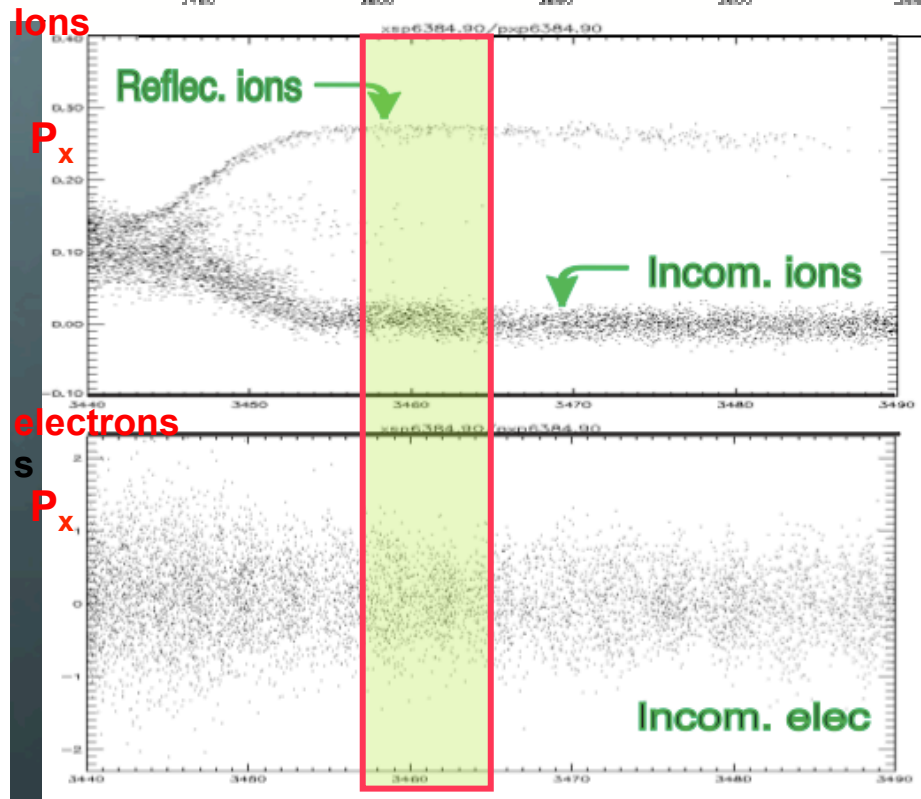
does self-reformation persist in presence of ECDI ?



# Basic ingredients for microturbulence in the foot



3 diff popul. (re. drift) --> Micro-instabi.



- MicroInst. --> add diffusion -> local heating  
--> impact of this diffusion on  
the self-reformation ?

\* Different types of micro-inst may be identified

	<b>Shimada et Hoshino ( 2002)</b>	<b>Schmitz et al. (2002, a,b)</b>	<b>Muschiatti et Lembege (2005) 2013</b>	<b>Scholer et al. (2003, 2004)</b>	<b>Scholer et Burgess (2005).</b>
<u>Instabilit</u>	Buneman	Buneman	El. Cycl Drift.	MTS	NonLinear whistler
<u>Shock angle</u>	90°	90°	90°	Oblique (87°)	Oblique (70°)
<u>source</u>	Refl. ions / elec.	Refl. ions / elec.	Refl. ions / elec.	Refl. ions/ elec.	Refl. ions/ Ions.
<u>Ma</u>	10.5	10.5	3	6	11
<u>Mi / me</u>	20 (low)	20 (low)	100 (256, 400)	1836 (real)	1836 (real)
<u><math>\omega_{pe}/\omega_{ce}</math></u>	20 (high)	20 (high)	2	2 (low)	2 (low)

SR persists

SR persists

SR persists

SR...differs

SR...differs

Self Ref. control by the instab.

Self Ref. control by the instab.



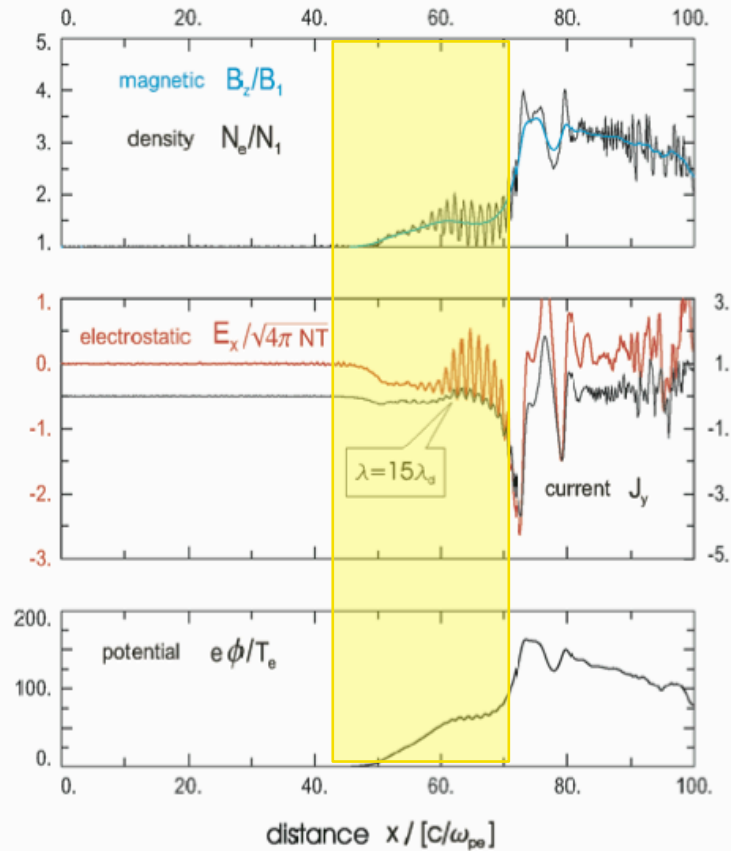


PIC simulations: composite snapshot

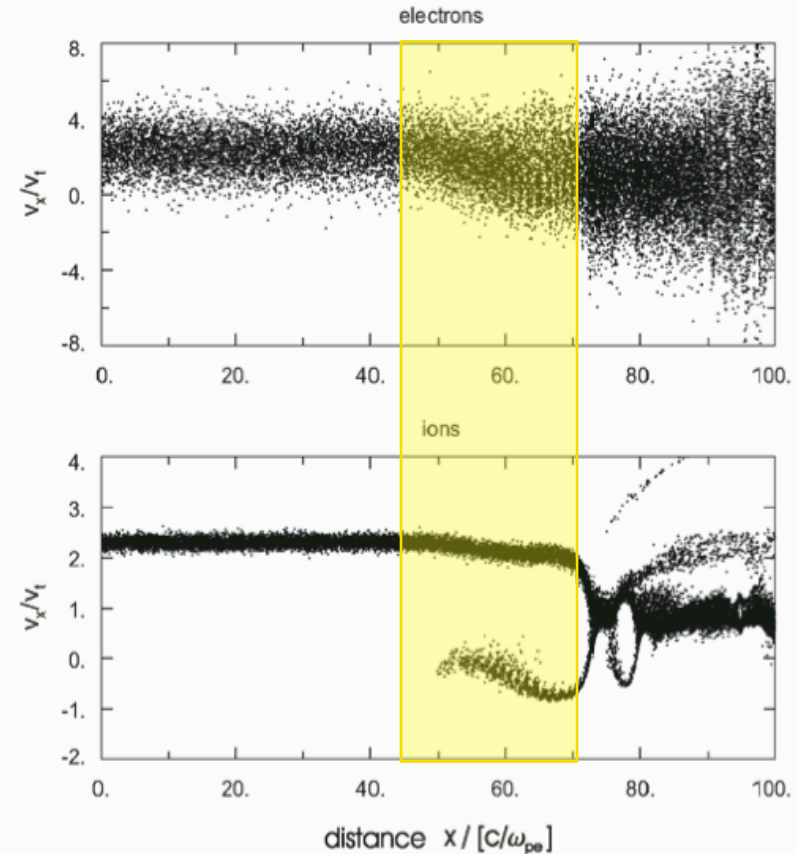
ECD Micro-inst. (Muschietti et Lembege, 2005)

( $\theta = 90^\circ$ ,  $Ma = 3$ ,  $R_{mass}=100$ ,  $\beta_e=0.035$ )  $\omega_{pe}/\omega_{ce}=2$

field quantities at  $\omega_{pe}t = 960$



particle phase space at  $\omega_{pe}t = 960$



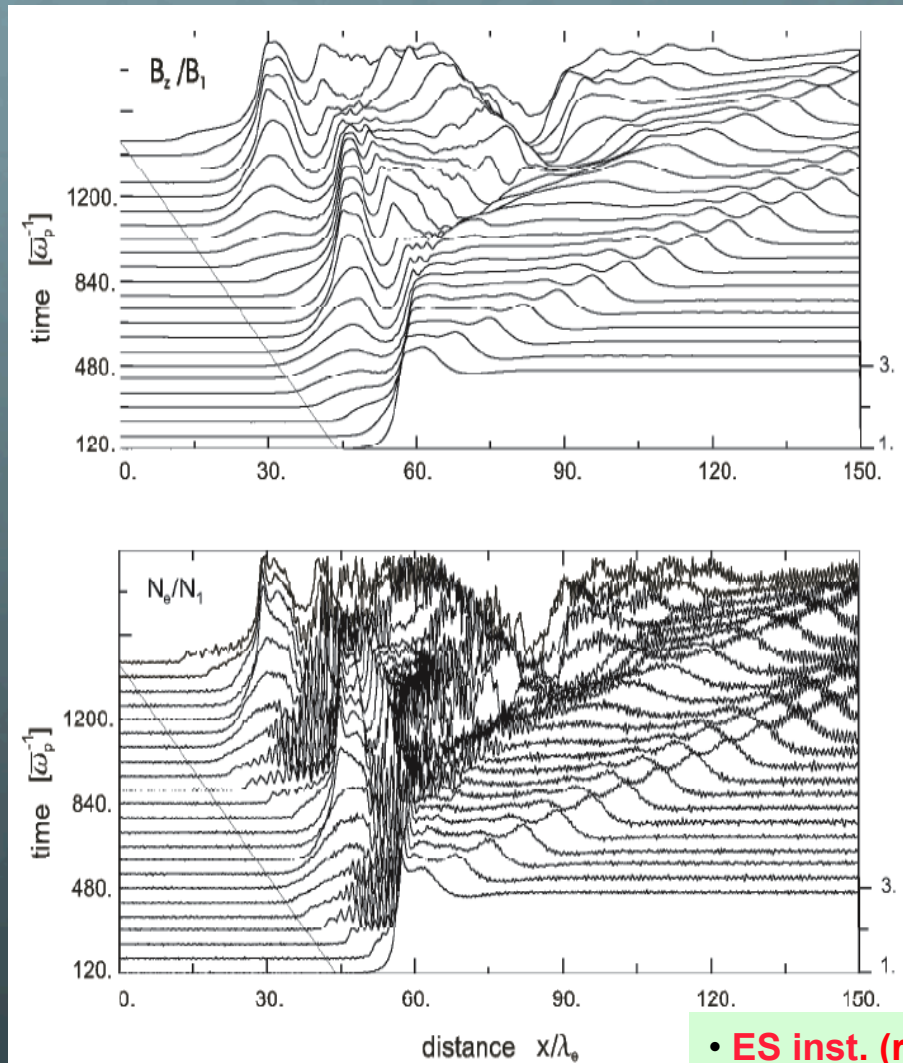
Mach number 3.0 upstream  $\beta_i=0.022$   $\beta_e=0.035$

--> ECDI is observed provided that the grid resolution is high enough

Does the ECDI suppress the self-reformation or not ??

## Sources of nonstationarity (Q-perp Shock)

ECDI (Muschietti et Lembège, 2006),  $\Theta = 90^\circ$



- **ES inst. (refle ions & elec.): coupl. of ion beam & Bernstein waves**
- \* Very rapid growth rate
- \* S.Ref. still driven by the accumul. of refl. ions
- accessib. to a **few  $10 \lambda_{De}$**  fluctuations within the foot



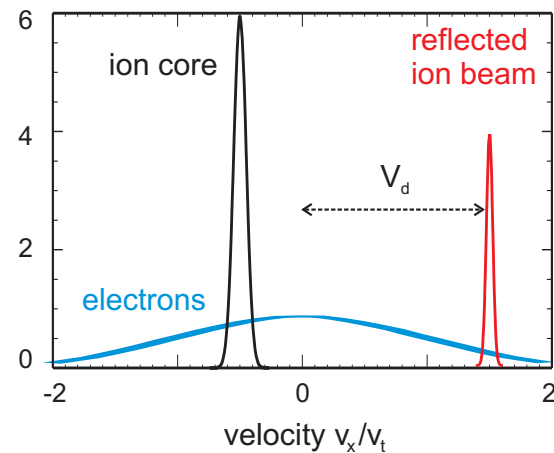
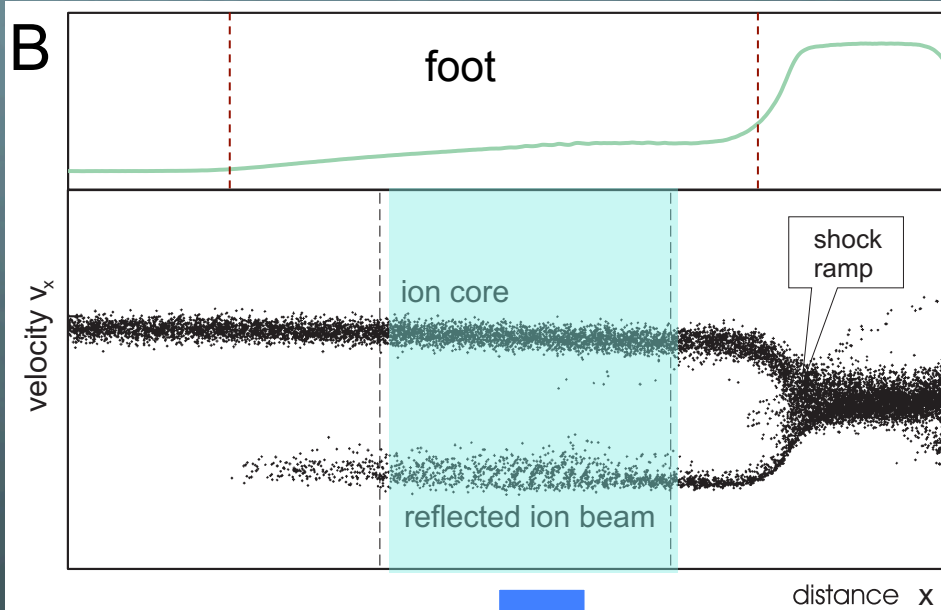
## Main questions :

- \* does self-reformation persist in presence of ECDI ?  $\rightarrow$  YES
- \* To account for wave activity within a shock front  $\rightarrow$  foot region
  - ECDI candidate OK ?
  - features of ECDI in L and NL stages ?
  - Do one recover signatures of ECDI in space experimental data ?

First approach (linear):  
dispersion relation

Second approach:  
PIC Numerical simulations

# Basic ingredients for microturbulence in the foot



Muschietti et Lembege, 2013

## Parameter choice

Symbol	Value
$\omega_{pe}/\Omega_{ce}$	10
$M/m$	400
$T_c/T_e$	1.
$T_b/T_e$	0.25
$V_d/V_A$	6

# Elements of the dispersion tensor

## ▶ Electrons as hot and magnetized

$$Q_{xx,e} = \frac{4\pi i}{\omega} \sigma_{xx,e} = -\frac{1}{k^2 \lambda_d^2} \left[ -1 + \Lambda_0(\eta) + 2 \sum_{n=1}^{\infty} \Lambda_n(\eta) \frac{\omega^2}{\omega^2 - n^2 \Omega_{ce}^2} \right]$$

where  $\eta \equiv (k\rho_e)^2 = (\omega_{pe}/\Omega_{ce})^2 (k\lambda_d)^2$

$\Lambda_n(\eta) \equiv I_n(\eta) \exp(-\eta)$ , modified Bessel function

## ▶ Ions as unmagnetized

$$Q_{xx,i} = \frac{4\pi i}{\omega} \sigma_{xx,i} = -\frac{\alpha}{k^2 \lambda_d^2} \frac{T_e}{2T_b} Z' \left( \frac{\omega - kV_d}{\sqrt{2}k v_{tb}} \right) - \frac{1 - \alpha}{k^2 \lambda_d^2} \frac{T_e}{2T_c} Z' \left( \frac{\omega - kV_c}{\sqrt{2}k v_{tc}} \right)$$

beam: drift  $V_d$ , thermal spread  $v_{tb}$  and relative density  $\alpha$

core: drift  $V_c = V_d \alpha / (\alpha - 1)$

## ▶ Perpendicular geometry here, electrostatic dispersion is simply

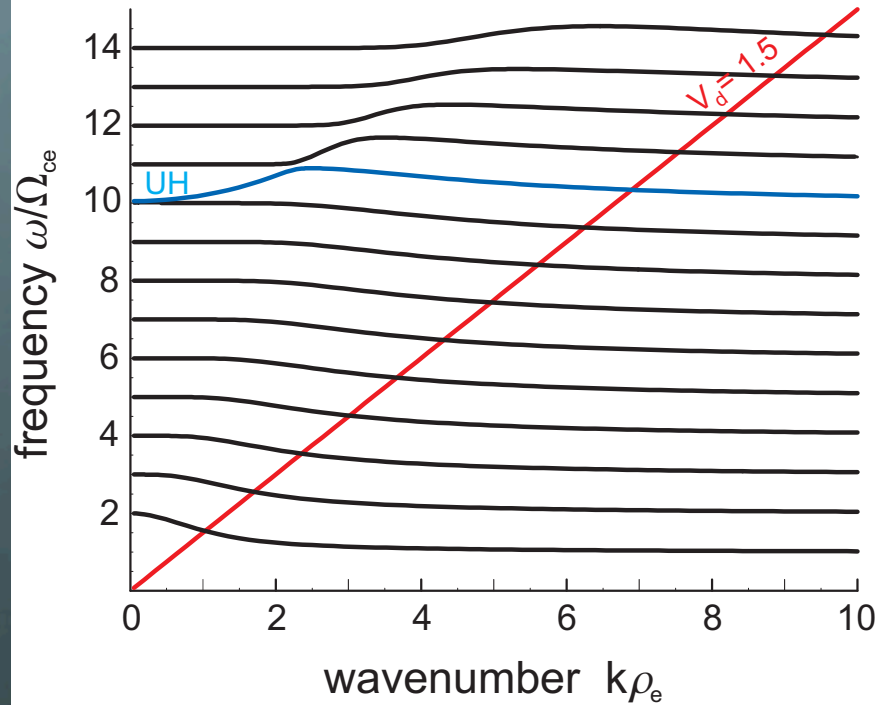
$$1 + Q_{xx,e} + Q_{xx,i} = 0.$$

ECDI : due to the relative drift between reflected ions and incoming electrons  
(coupling between ion beam and electron Bernstein waves)

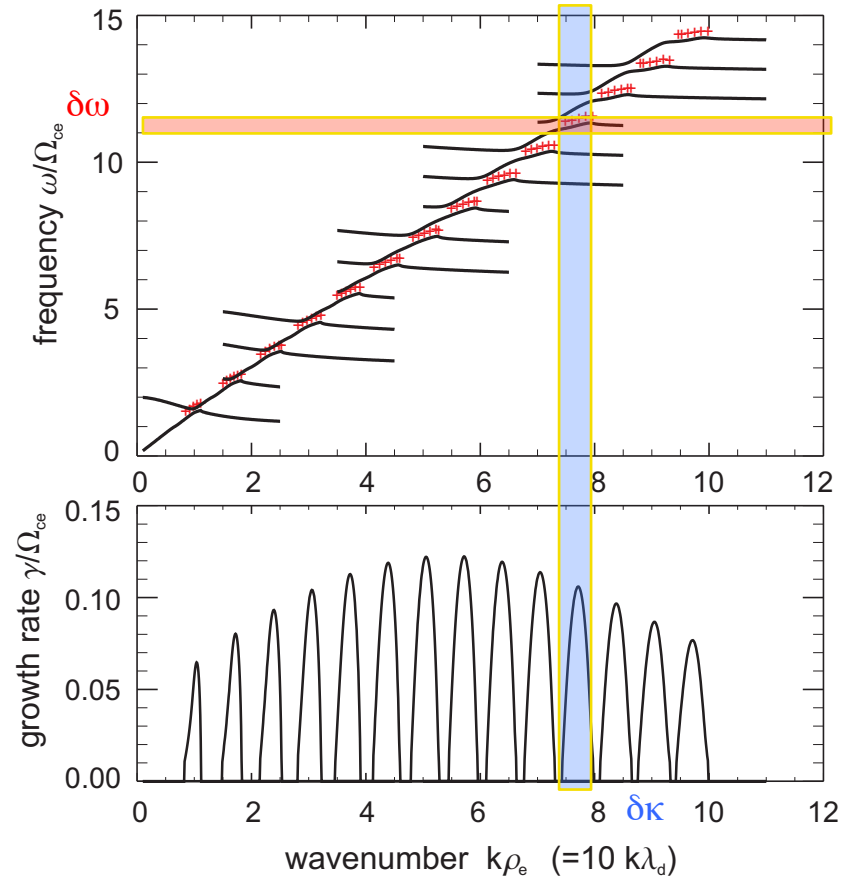


# Electron Cyclotron Drift Instability

Before coupling



After coupling



- \* Discrete bands in spectrum
- \* Peaked envelope  $\rightarrow$  high  $k$  excited first, lower  $k$  excited later.....

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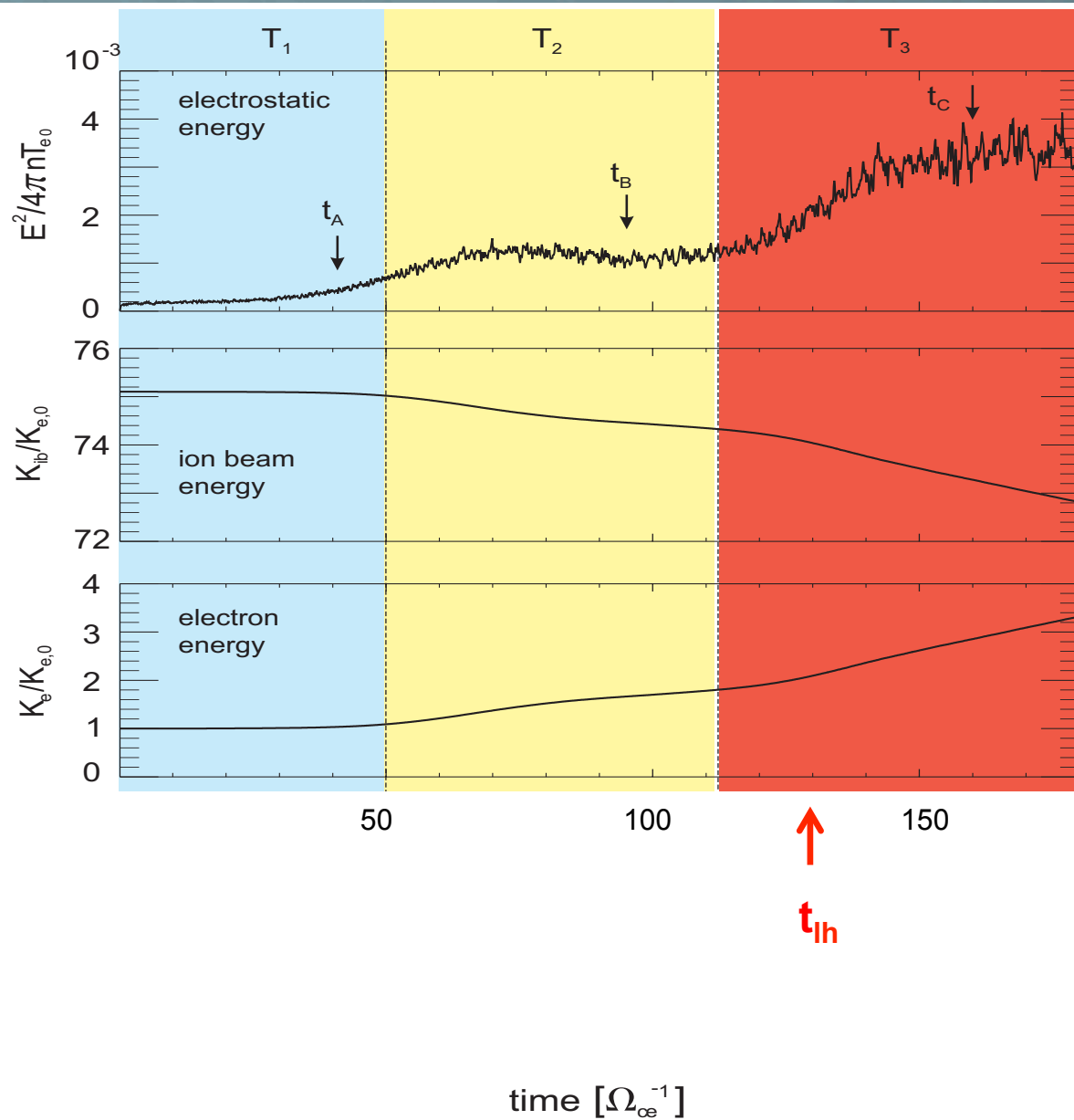
Second approach:  
PIC Numerical simulations

Separate periodic 1D PIC simulations with:

- \* Ion core
- \* Ion beam
- \* Electrons

$\rightarrow$  To analyze in details the L / NL stages of the ECDI

# Evolution of Electron Cyclotron Drift Instability



## Main results

a) 3 stages :

\* Linear  $T_1$

\* Nonlinear:  $T_2$  and  $T_3$   
(redistribut to lower k modes)

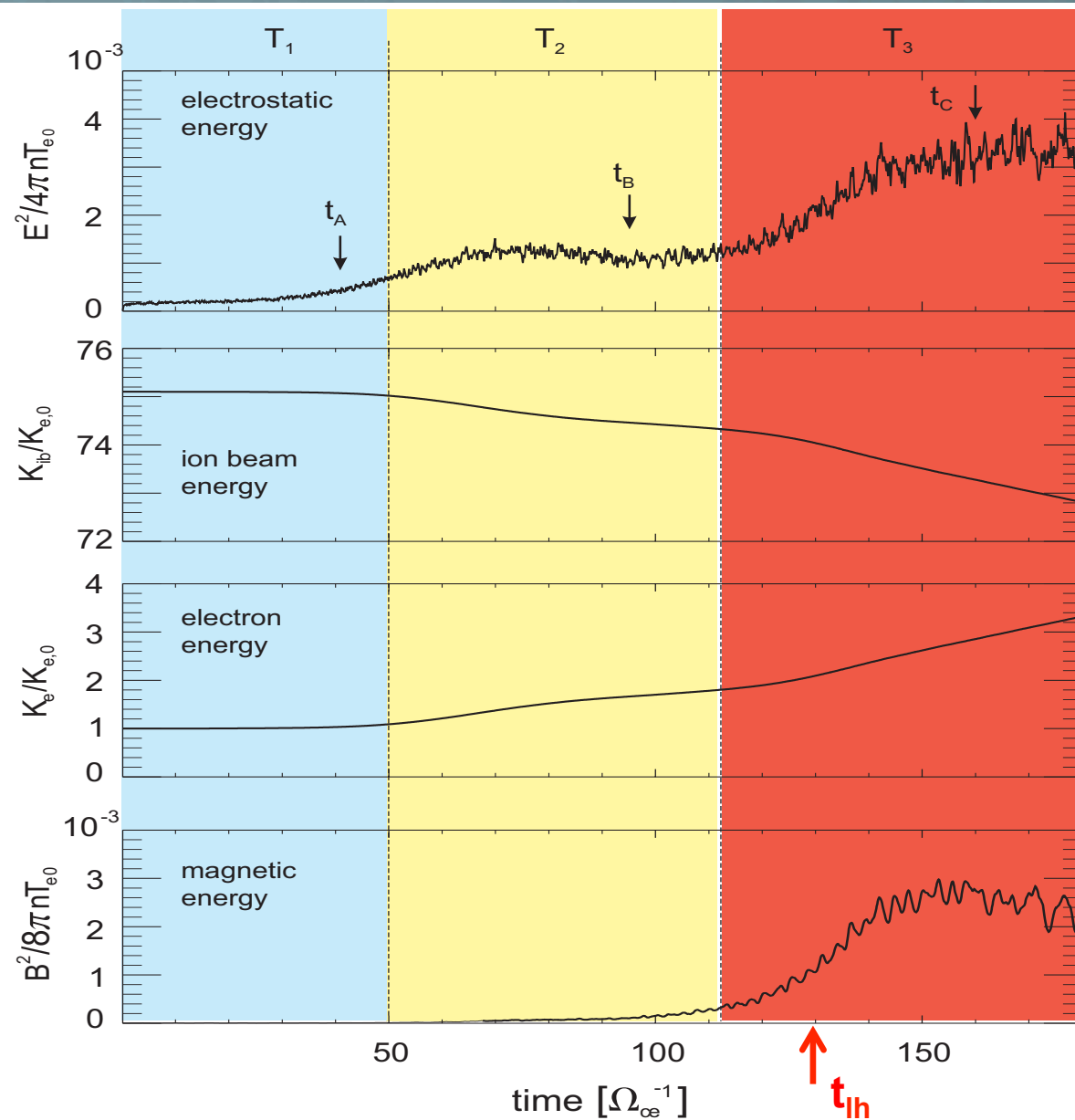
b) transfert of ion beam energy  
-> to electrons

→ Ion beam only loses a few %

c) Rapid growth and NL stage ( $t < T_{lh}$ ) .....  $\ll T_{ref} < T_{ci}$



# Evolution of Electron Cyclotron Drift Instability



## Main results

a) 3 stages :

\* Linear  $T_1$

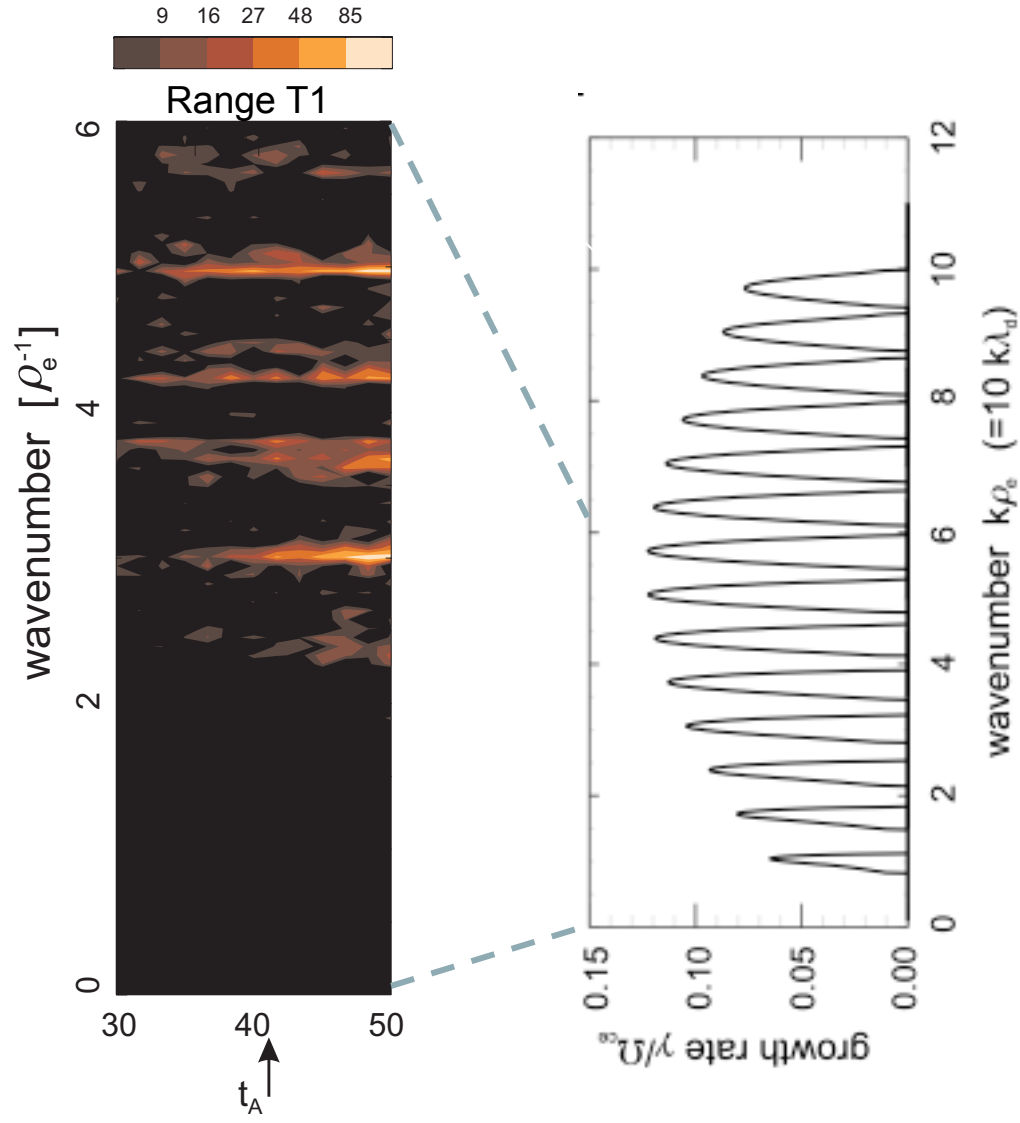
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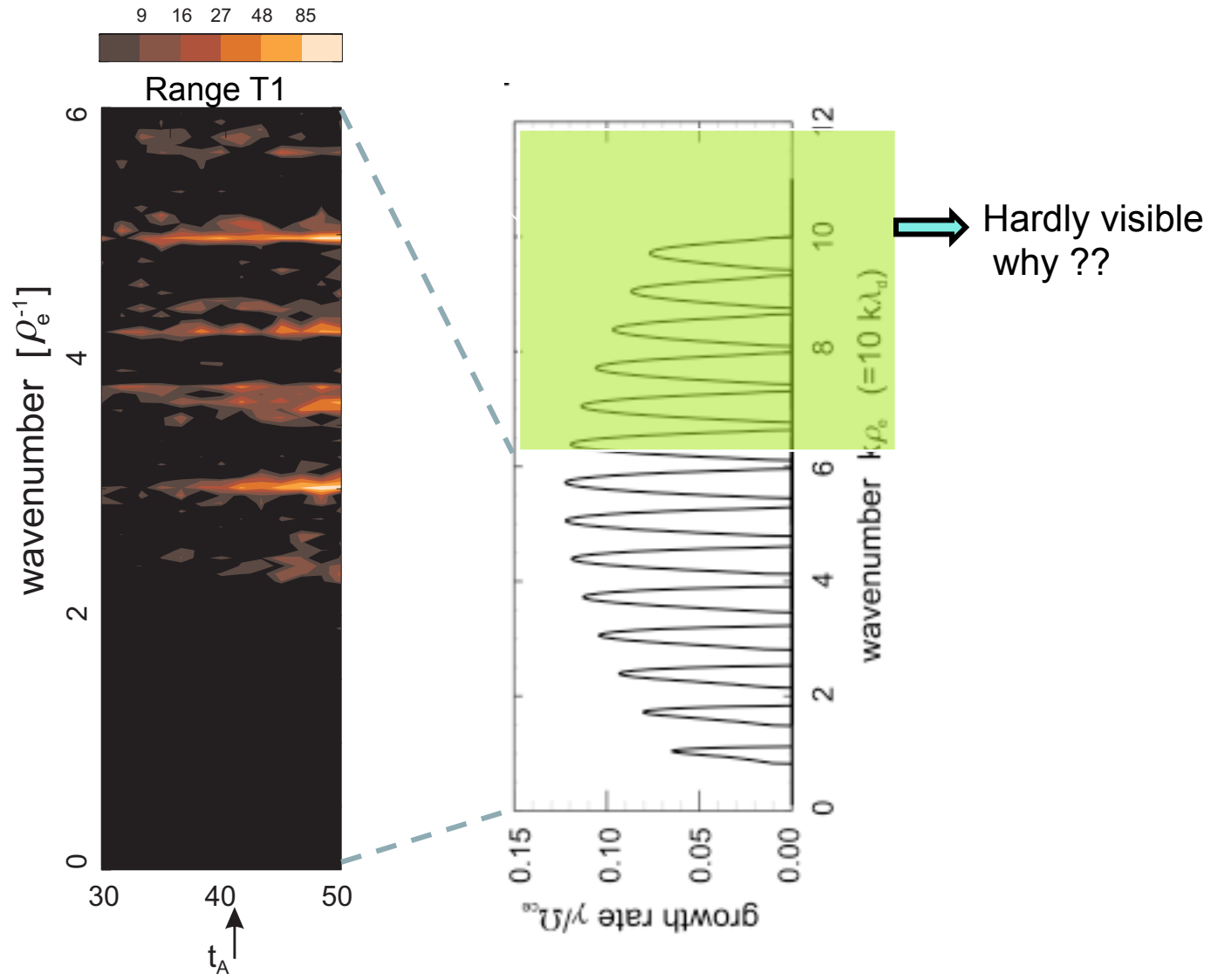
c) Rapid growth and NL stage ( $t < T_{Ih}$ ) .....  $\ll T_{ref} < T_{ci}$

d) **Magnetic component during stage  $T_3$ ..!!**

# Time history of the electrostatic spectrum

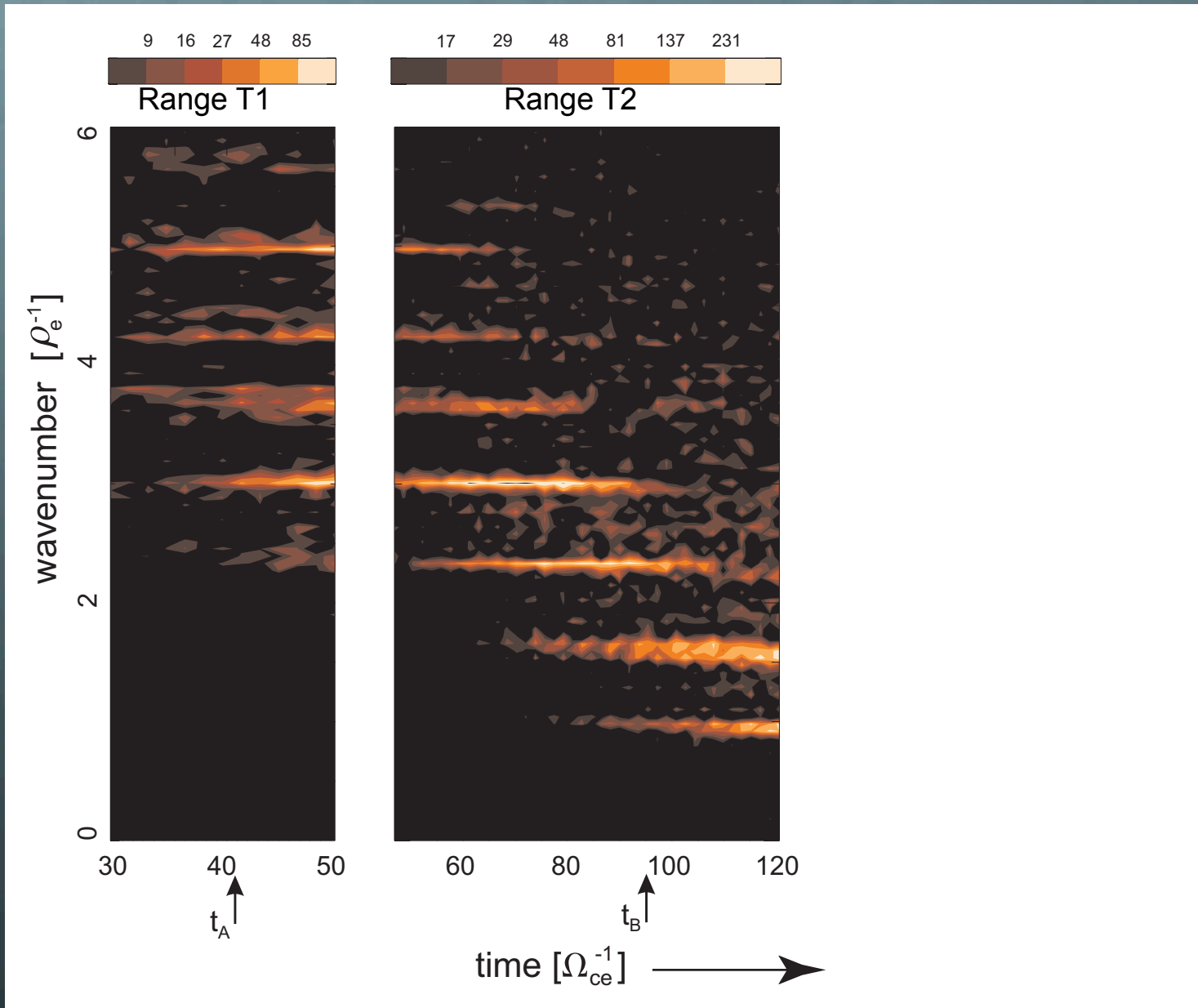


# Time history of the electrostatic spectrum

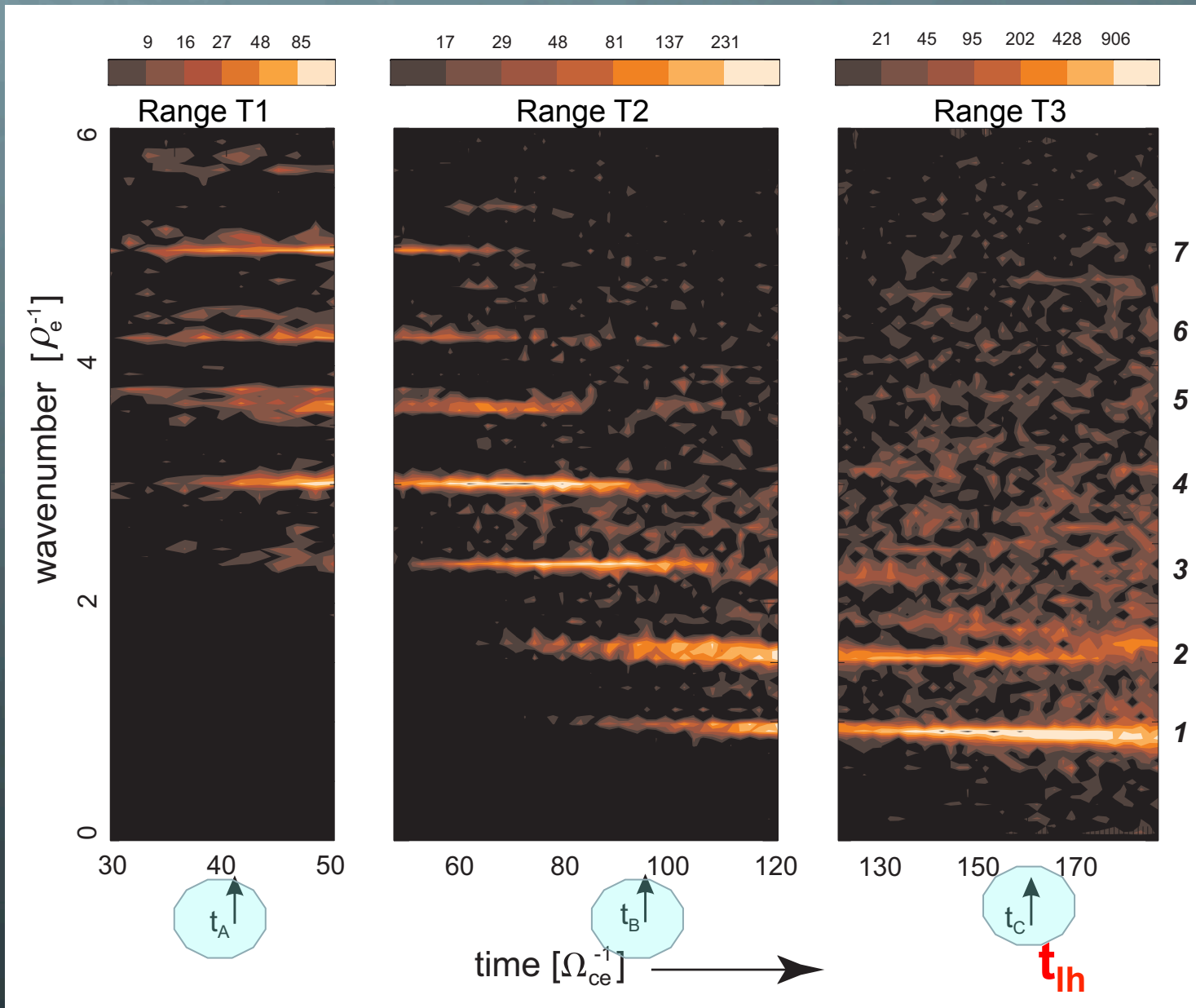




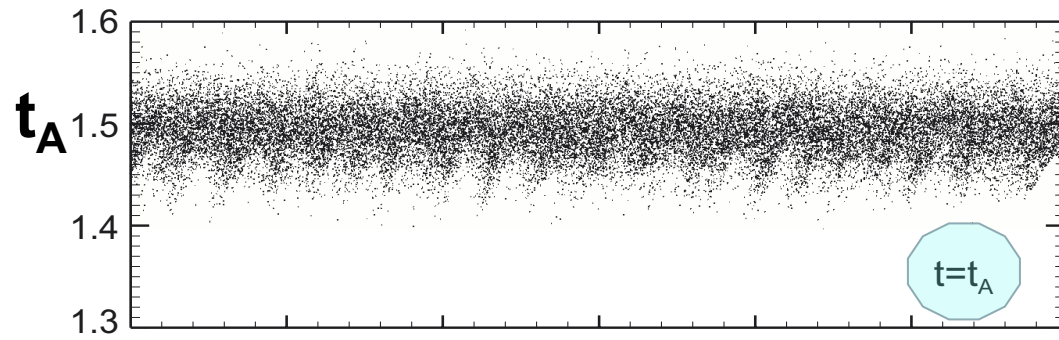
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# Time history of the electrostatic spectrum



# Evolution of the Ion Beam

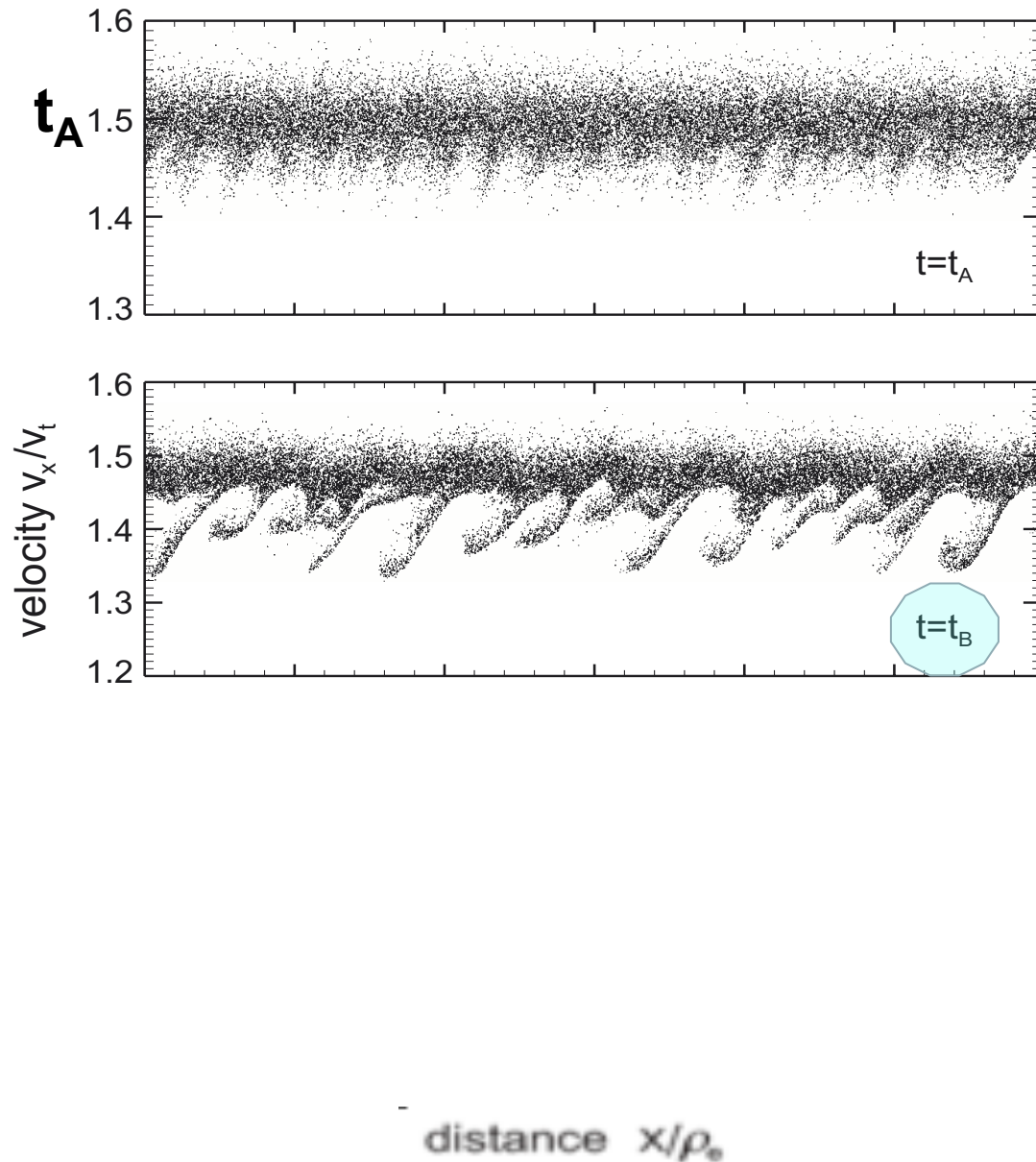


Ion deceleration

distance  $x/\rho_e$



# Evolution of the Ion Beam



**Ion deceleration**

**Bounce frequency:**

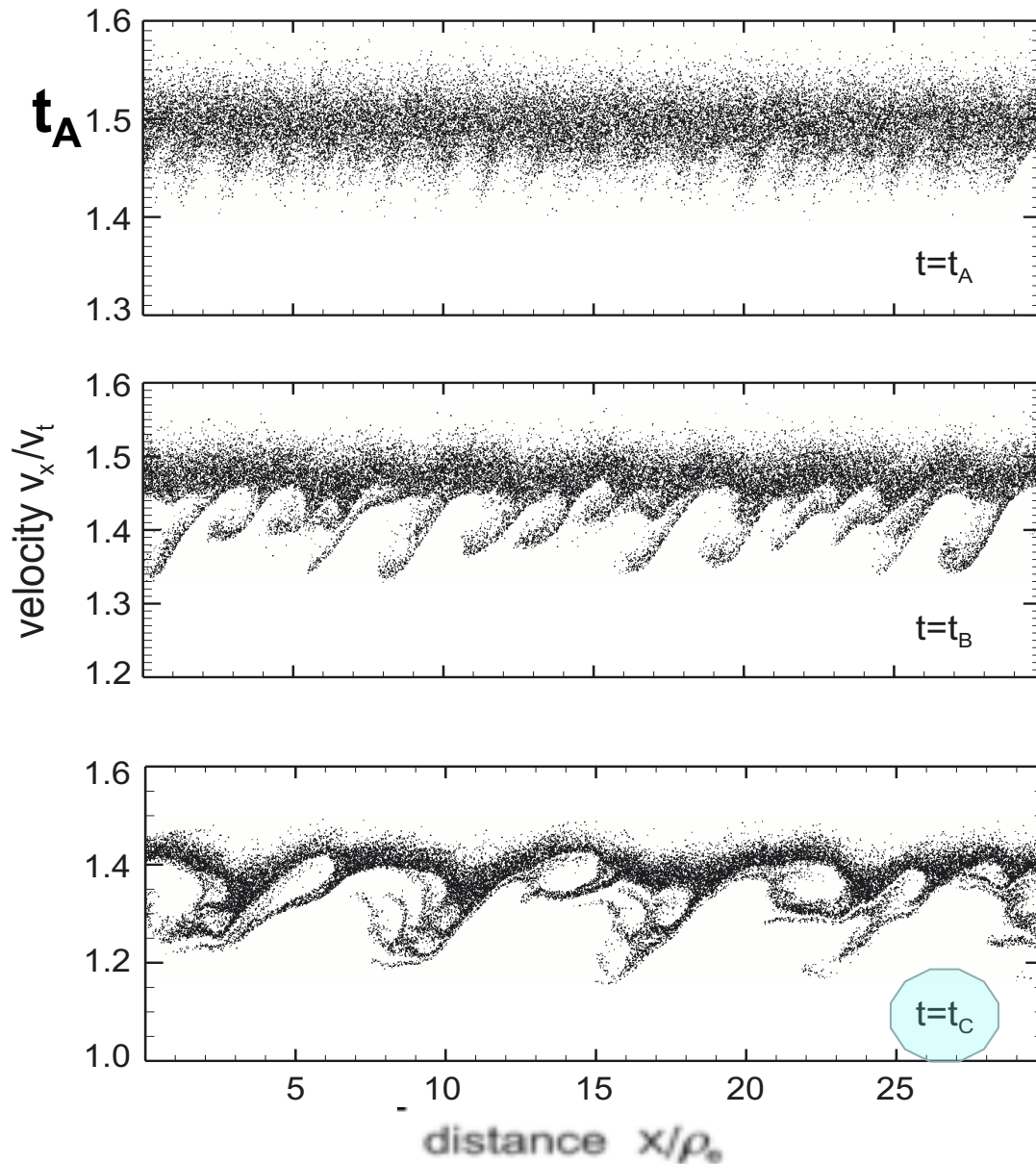
$$\sqrt{\frac{eE}{M}} k$$

**trapping begins earlier**

**for high-k modes**

**When trapping at low-k begins  
high harmonics lose  
coherence**

# Evolution of the Ion Beam



**Ion deceleration**

**Bounce frequency:**

$$\sqrt{\frac{eE}{M}} k$$

**trapping begins earlier**

**for high-k modes**

**When trapping at low-k begins  
high harmonics lose  
coherence**



**Waves spectrum at high  
harmonics is reabsorbed**

**Harmonic 1 at  $\Omega_{ce}$  grows and  
dominates the spectrum**

**Why high-k modes disappear at very late times ?  
(....i.e. why only fundamental harmonic  $\omega_{ce}$  survives ?**



**Signature of « inverse cascade » process ?**

**Why high-k modes « die out » at very late times ?  
(....i.e. why only fundamental harmonic  $\omega_{ce}$  survives ?**



**Signature of « inverse cascade » process ?**



**NO**



**Two effects contribute .....**  
**“Resonance broadening” vs “ion trapping”**



# Resonance Broadening

[Dum and Dupree, 1970; Lampe et al., 1972]

Electron orbits in ambient magnetic field  $(0, 0, B_0)$

- ▶ Linear orbit: In plane  $[x, y]$  gyrocenter, gyroradius, gyrophase well defined
- ▶ Orbit in turbulent medium: Brownian motion of gyrocenter, random changes in gyroradius and phase angle
  - limits wave-electron interaction time to  $\tau_D$
  - broadens resonance in dispersion relation

$$Q_{xx,e} = -\frac{\omega_{pe}^2}{k^2} \int d^3v \left[ 1 - \sum_{n=-\infty}^{\infty} \frac{\omega J_n^2(kv_{\perp}/\Omega_{ce})}{\omega - n\Omega_{ce} + i\Delta\omega_k} \right] \frac{1}{v_{\perp}} \frac{\partial f_e}{\partial v_{\perp}}$$

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Broadening  $\Delta\omega_k \equiv Dk^2$  with  $D \sim \sum_{k'} \frac{|E_{k'}|^2}{4\pi nT_e}$  diffusion coefficient of electrons.

Effect is stronger for high wavenumbers → loss of coherency in gyromotion

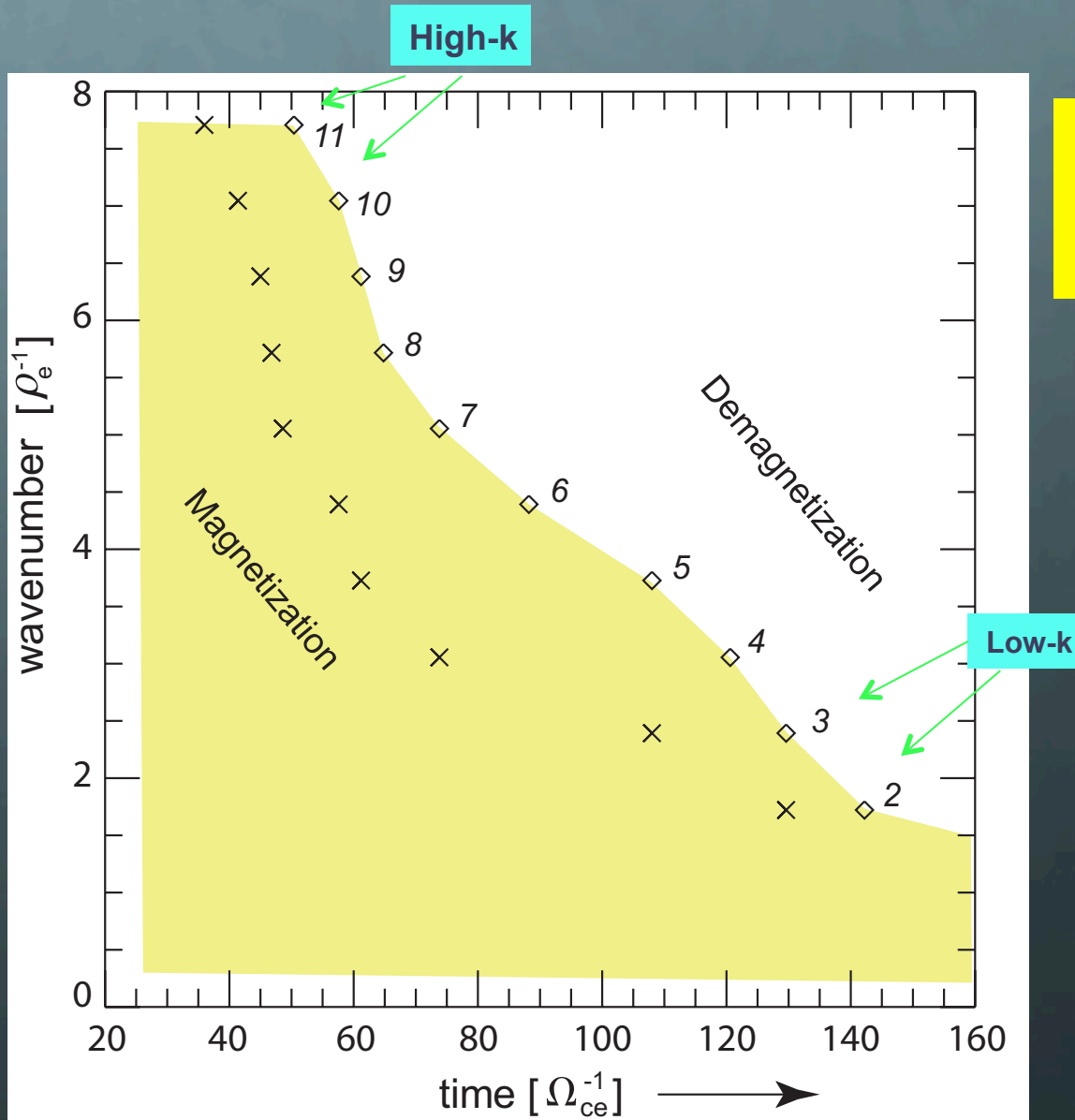
For high  $k\rho_e$  ( $k\rho_e \gg 1$ ) demagnetization of electrons when

$$\tau_D (= \langle \Delta\omega_k \rangle^{-1}) < (\Pi / \Omega_{ce}) \quad \langle \dots \rangle: \text{average over } F_e$$

→ Interplay with ampl. of turb ( $E_{k'}^2$ ) and k order.

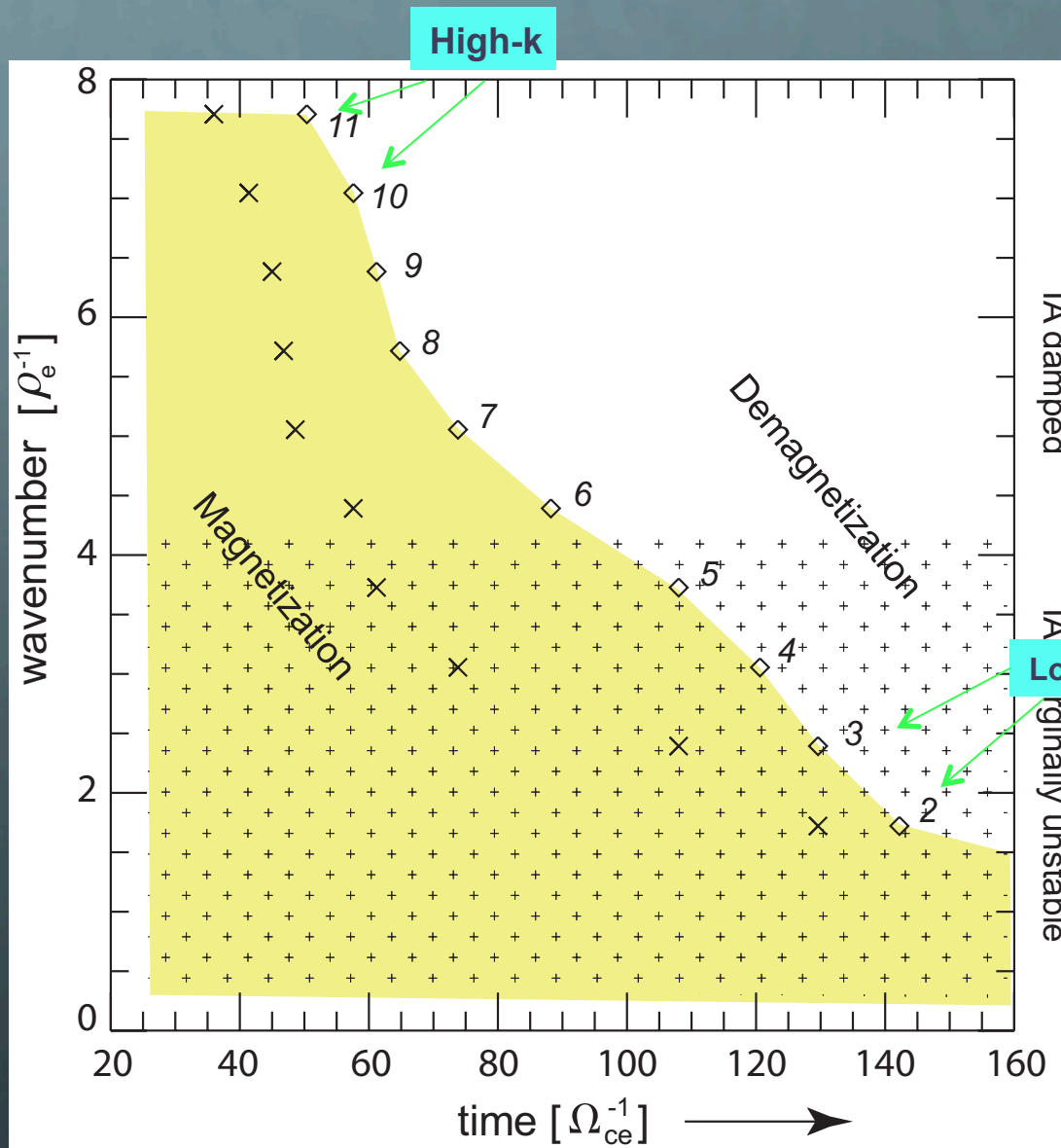
# Stabilization by Resonance Broadening

Muschiatti et lembège, 2013



As time increases, demagnetization proceeds from high-k to low-k

# Stabilization by Resonance Broadening



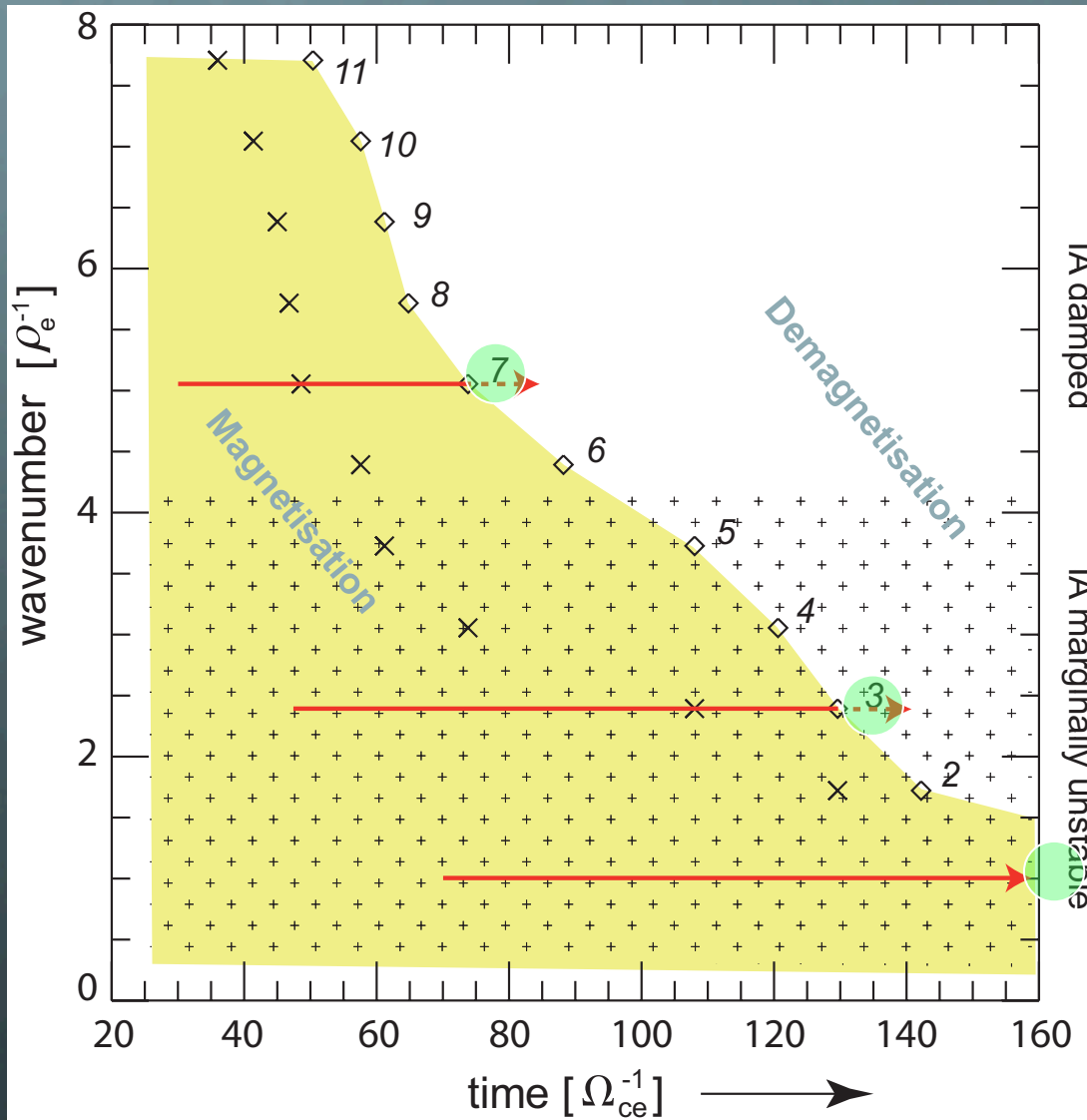
As time increases,  
demagnetization proceeds  
from high-k to low-k

Magnetized dispersion  
disallowed...  
No ECD  
(Ion acoustic ?)



# Stabilization by Resonance Broadening

As time evolves, turbu. level increases



As time increases, demagnetization proceeds from high-k to low-k

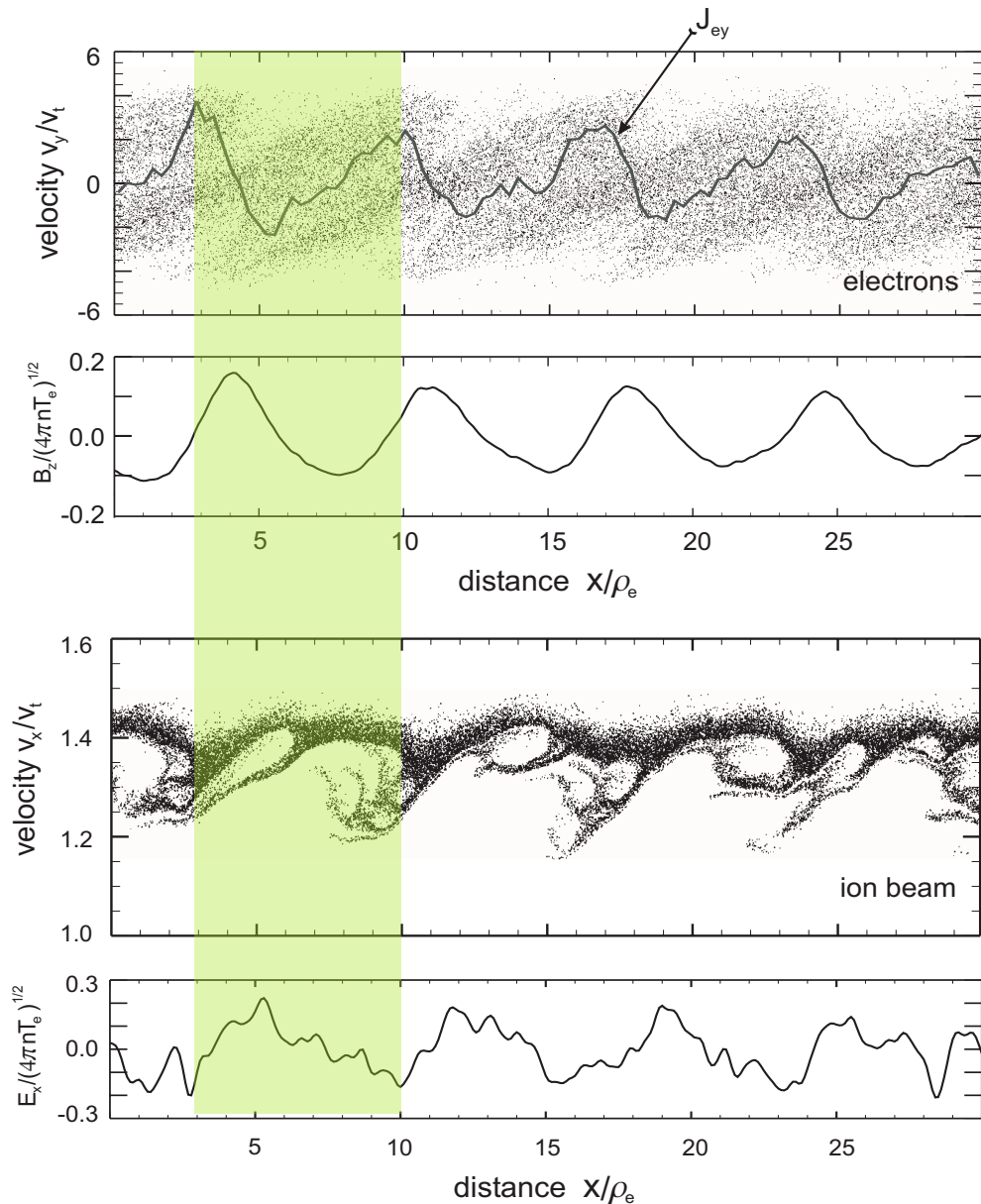
Magnetized dispersion disallowed...  
No ECD  
Ion acoustic?

ECD survives only for **harmonic 1** at  $\Omega_{ce}$

Origin of the magnetic field growth in nonlinear  
T<sub>3</sub> stage

→ Electron current ?

## Magnetic signatures of the waves: nonlinear stage T3



\* “enlarged” snapshot at  $t = t_c$  (stage T3)

\* cross-field forces on electrons

$$(B_{0z} \times E_x)$$



\* Create current  $J_{ey}$  (by integrating electrons)

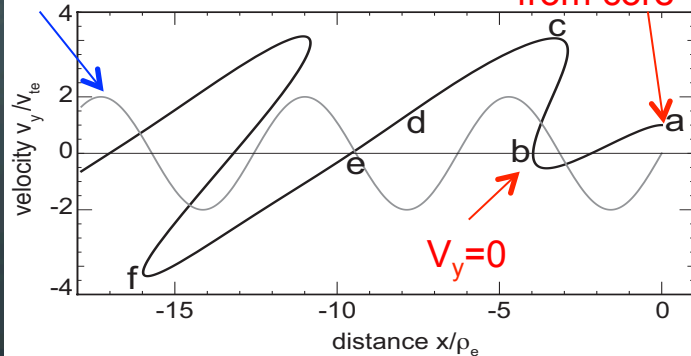
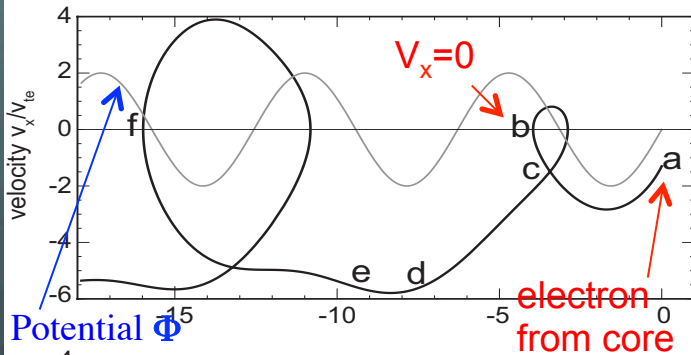
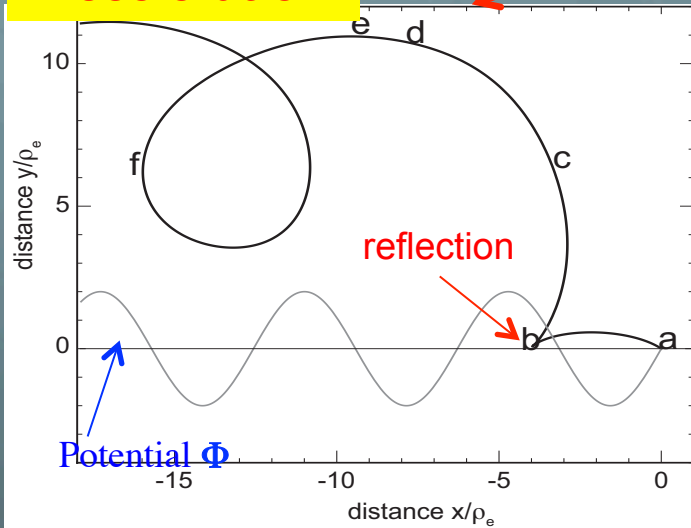
\* Most electrons in the range  $(2 < v_y < 4)$  contribute to  $J_{ey}$

\*  $J_{ey}$  fluctuations fits with largest scale (in ion beam) which dominates at late time

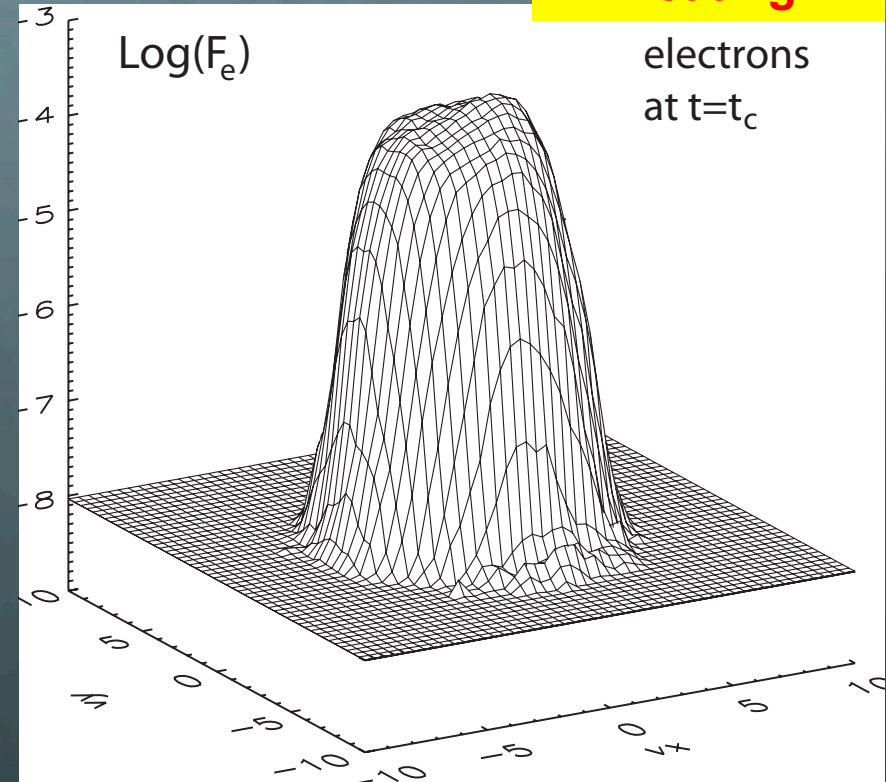
\* Spread electrons in  $[v_x, v_y]$  space  
**-> heating**

# electron dynamics in a Bernstein wave (with $\omega = 1.3 \omega_{ce}$ )

## Acceleration



## Heating



$t_c \sim$  lower-hybrid period  $\ll T_{MTSI}, \tau_{ref}$

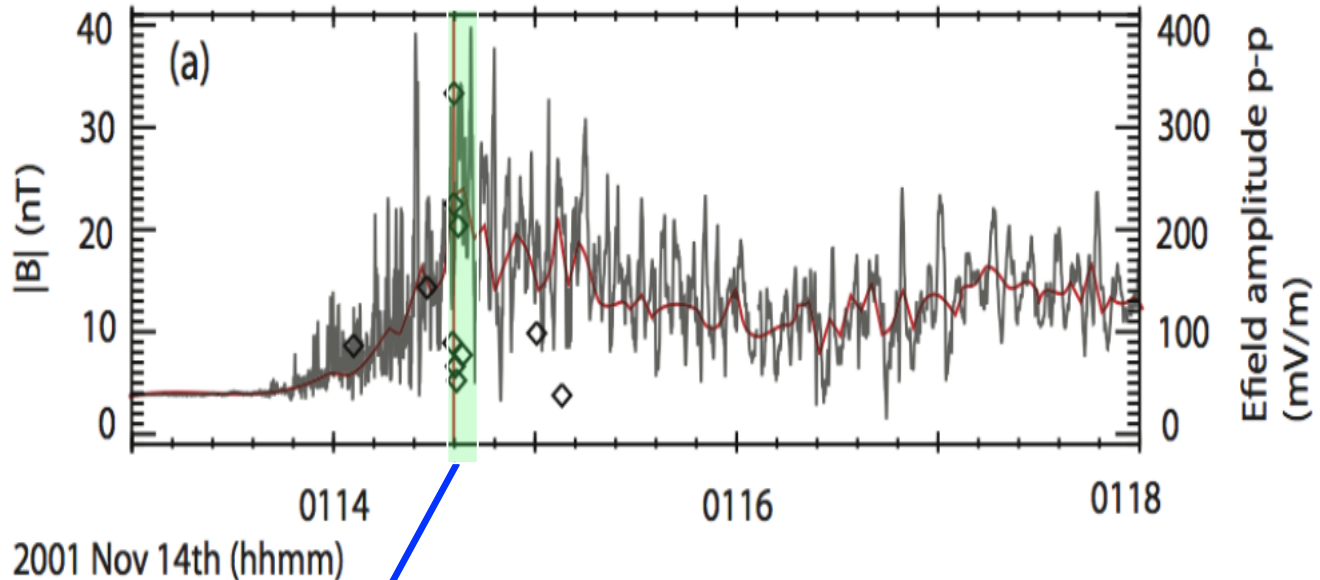
- \* electron preheating
- \* Distribution gets rapidly "flat top" shape

Is ECDI microturbulence observed in exp. data ??

**YES !!**

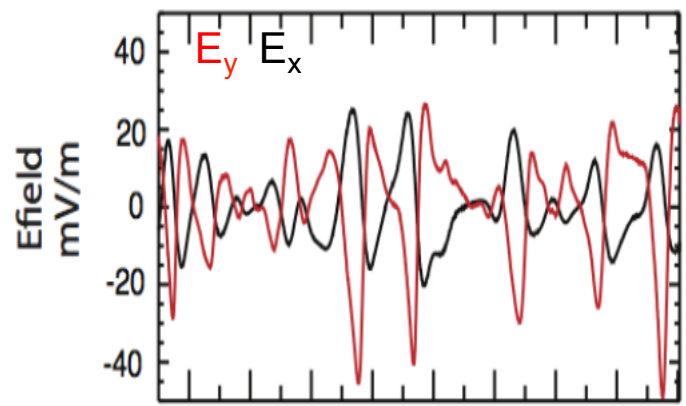


# WIND Observations (Breneman and al.; 2013), bow shock crossings

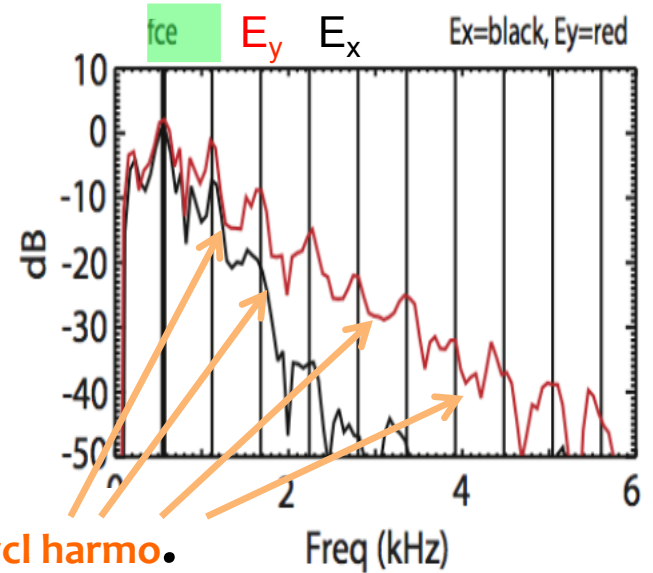


- \* Peaks around the  $n\Omega_{ce}$
  - \* No harmonics along  $B_0$
  - \* Emission decays as order  $n$  decreases
- With a strongest emission at fundam.  $\Omega_{ce}$

Waveform capture (for E field)



Spectrum of Waveform capture



Elec. Cycl harmo.

## Conclusions:

i) **ECDI**: Strong and quick emission in the electron cyclotron range → discrete energy spectrum (no continuum) → signature of Bernstein waves ... ..within  $t_{ih} \ll t_{ref}$

ii) Electrostatic spectrum → temporal accumul of energy on the fundamental ( $\omega_{ce}$ ) («NO inverse cascade» process). Two effects contribute:

a) « ion trapping » takes place but applies at diff times on diff. K modes (from high to low K modes)

b) «resonance broadening» applies to high (early time) and to low K (later time) → electrons demagnetisation.

iii) Energy transfert from ion beam → electrons (flat-top distri function) → «Electron preheating » in the foot (Te/Ti diff . versus US conditions)

iv) Magnetic component in NL regime (due strong  $E \times B$  to electrons peaked  $J_y$  → induces  $B_{tz}$ )

v) In course.. comparative analysis between....



**ECDI**

....90° and slightly oblique



**MTSI**

....oblique

.. extension to MMS data ..

